# Experimental Disaggregation of Propagation Effects in Optical Links

J. Girard-Jollet<sup>1</sup>, J.-C. Antona<sup>1</sup>, A. Carbó Meseguer<sup>1</sup>, F. Boitier<sup>2</sup>, P. Ramantanis<sup>2</sup>, G. Rekaya<sup>3</sup>

<sup>1</sup>Alcatel Submarine Networks, 1 Av. du Canada, 91940 Les Ulis, France, <u>joana.girard\_jollet@asn.com</u>, <sup>2</sup>Nokia Bell Labs, 12 rue Jean Bart, 91300 Massy, <sup>3</sup>Télécom Paris, 19 Pl. Marguerite Perey, 91120 Palaiseau

**Abstract:** We introduce a protocol to evaluate experimentally the fiber nonlinear coefficients for intra- and inter-channel effects. We characterized a three-span transmission using highly dispersed QPSK signals, observing good agreement with the eGN model. © 2024 The Author(s)

# 1. Introduction

Accurate quality of transmission (QoT) estimation has become essential for optical networks to reduce margins during network design. For a decade, the enhanced Gaussian noise (eGN) model [1] has become the reference in the optical network community for nonlinearity modeling. eGN model allows evaluating separately intra-channel nonlinear effects, or self-phase modulation (SPM), and inter-channel nonlinear effects, or cross-phase modulation (XPM). However, the experimental validation of these models is complex as it targets nonlinear noise accumulation, which is, in practice, difficult to evaluate for real systems in transmission operation. In literature, the eGN model has been experimentally validated and also refuted by different research groups, as described in [2]. Usually, for model validations, the aggregation of all the propagation effects is measured in transmission and compared to the model prediction. Thus, the noise targeted can be hidden by other noises. Indeed, it is difficult to evaluate each effect for long haul systems as spectral haul burning (SHB) smooths the power profile, and thus, it is complex to control the stimulation of XPM and SPM.

Thus, this paper aims to present a methodology to isolate the different propagation effects, such as the SPM and XPM noises, as well as an additional source of noise characterized by a signal-to-noise ratio (SNR) term independent of power. We experimentally isolated each effect in a few-span transmission link that could be representative of a long-haul system. Having only three spans allows us to avoid amplifiers SHB, and we could vary the input power in different single- and multi-channel configurations, over wide ranges of power. All modulated channels were pre-dispersed with 10ns/nm to operate in a dispersive regime typical of long-haul propagations. The measured SPM and XPM noise variances are compared with the eGN model predictions, showing good agreement, and the additional source of noise could correspond, according to the calibration done in [5,6], to the Guided Acoustic Wave Brillouin Scattering (GAWBS) penalty and the equalization enhanced phase noise (EEPN).

## 2. Experimental investigations setup

The experimental setup is presented in Fig. 1. The transmission line consists of three spans of SMF of 100 km each, an attenuation of 0.21 dB/km, 80- µm2 effective area, and a chromatic dispersion of 16.7 ps/nm/km. We used dualstage erbium-doped fiber amplifiers (EDFAs) with an output power per channel ranging between -5 and 10 dBm. Fifteen dual-polarization (DP) QPSK channels were modulated at 32 GBd with a spacing of 50 GHz using three different offline transponders properly decorrelated to avoid non-desirable correlation effects. OPSK channels were shaped by a root-raised-cosine filter with a 0.01 roll-off factor, and the central channel, the channel of interest (COI), was inserted at 1545.4 nm. At emission, we applied a digital chromatic dispersion pre-distortion of 10 ns/nm to the signal. The pre-distortion was to ensure we had a constellation with Gaussian statistics at reception. The SNR was not computed from the measured bit error rate (BER) (too few errors after the propagation to measure a BER in a reasonable time) but with the error vector magnitude (EVM) method. EVM is the root-mean-square value of the difference between the collection of measured symbols and ideal symbols. However, the EVM method is rigorously valid only for a constellation with Gaussian statistics at reception [3]. At the reception, we estimated the SNR with ten oscilloscope acquisitions after the coherent mixer. We also measured the COI's optical SNR (OSNR), which accounts for the amplified spontaneous emission (ASE) noise. The OSNR was measured with an optical spectrum analyzer and by replacing the COI with a depolarized laser to access the actual ASE noise floor, as presented in [4]. Additionally, the power spectrum was measured at the output of each EDFA. The transceiver penalty was characterized through back-to-back transmissions as described in [4], where the SNR was measured for different levels of ASE noise. The SNR<sub>TRx</sub> was estimated at 21.3 dB. It permitted isolating SNR<sub>EXT</sub> using the formula in [4]. SNR<sub>EXT</sub> is like the GSNR but also includes the noise caused by the transceiver due to propagation specific effects such as EEPN. In the following, we call variance the inverse of the SNR.



Fig. 1. Experimental setup for the propagation of 15 channels on the 300-km line.

We studied the transmission of different power profile configurations with 15 channels shown in Fig. 2. There are: 1)  $P_{FLAT}$ : a flat power profile and each channel power varies from -5 to 10 dBm; its nonlinear threshold is P(NLT)

2) P<sub>CUT</sub>: the COI varies from -5 to 10 dBm while the 14 adjacent channels remain at P(NLT),

3) PADJ: the adjacent channels vary from -5 to 10 dBm while the COI remains at P(NLT),

4)  $P_{1CH}$ : a pseudo-single channel transmission where the COI varies from -5 to 10 dBm. The adjacent channels are on the edge of the amplifier's bandwidth, 1.5 THz away from the COI to emulate a single channel transmission.

## 3. Protocol to obtain the nonlinear coefficients

The optical transmission total variance is the sum of three contributions:  $var_{TOT} = var_{ASE} + var_{NLI} + var_{res}$  (=1/SNR<sub>EXT</sub>). var<sub>ASE</sub> accounts for the ASE noise,  $var_{res}$  accounts for the residual noise whose variance is independent of power, (like GAWBS and EEPN penalties), and  $var_{NLI}$  accounts for the nonlinear noise, which variance scales like the square of the power:  $var_{NLI} = \alpha_{SPM} * P_{COI}^2 + \beta_{XPM} * P_{WDM}^2$ , with  $\alpha_{SPM}$  and  $\beta_{XPM}$  the coefficients for SPM and XPM, respectively, and  $P_{COI}$  the power on the COI and  $P_{WDM}$  the averaged power on the 14 adjacent channels.

We aim to estimate  $\alpha_{SPM}$  and  $\beta_{XPM}$  experimentally, assess their reproductivity by testing different configurations, and compare them to the predictions of the eGN model. Additionally, we estimate var<sub>res</sub> and compare it to the simulation tool's prediction for EEPN and GAWBS.

The first step is to remove the ASE noise contribution that we obtained through the OSNR measurements to the total noise, and we do so for each configuration:  $var_{TOT-ASE} = var_{TOT} - var_{ASE}$ . We obtain for the four configurations:

 $P_{FLAT}: var_{TOT-ASE} = var_{res} + \alpha_{SPM}*P_{COI}^2 + \beta_{XPM}*P_{WDM}^2 \qquad P_{ADJ}: var_{TOT-ASE} = var_{res} + \alpha_{SPM}*P(NLT)^2 + \beta_{XPM}*P_{WDM}^2 \qquad P_{ADJ}: var_{TOT-ASE} = var_{res} + \alpha_{SPM}*P(NLT)^2 + \beta_{XPM}*P_{WDM}^2 \qquad P_{1CH}: var_{TOT-ASE} = var_{res} + \alpha_{SPM}*P_{COI}^2 + XPM_{edge\_channels} \qquad We obtain \alpha_{SPM} with P_{1CH} and P_{CUT} as these are the transmissions for which P_{COI} varies, and thus, SPM dominates at high power. We use a linear function fit to determine <math>\alpha_{SPM}$  from P<sub>CUT</sub> and P<sub>1CH</sub>. Similarly, we use P<sub>ADJ</sub> to obtain  $\beta_{XPM}$  as it is a configuration for which P<sub>WDM</sub> varies and, at high power, the XPM is predominant. Then, using  $\alpha_{SPM}$  and  $\beta_{XPM}$ , we remove the estimated SPM plateau,  $\alpha_{SPM}*P(NLT)^2$ , from P<sub>ADJ</sub> and the XPM plateau,  $\beta_{XPM}*P(NLT)^2$ , from

 $P_{CUT}$ . We also remove the plateau due to the XPM from the amplifier's bandwidth edge channels, XPM<sub>edge\_channels</sub> (estimated with the eGN model at -42.5 dB), from  $P_{1CH}$ . Lastly, we search for the remaining var<sub>res</sub> that minimizes the overall distance to the experiments var<sub>TOT-ASE</sub> of  $P_{1CH}$ ,  $P_{CUT}$ ,  $P_{ADJ}$ , and  $P_{FLAT}$ .

## 4. Experiments results and comparison with the model

For the transmissions, the COI's power was always within less than 0.1 dB of the target power. On the other hand, the input power profile tilt was optimized such that, on average, on the three spans, the power on each channel was within less than 0.2 dB of the target. We also consider the connector losses at the output of the amplifiers which were equivalent to -0.96 dB at each span. Using the experimental calibrations obtained from [5] we obtained  $var_{GAWBS} = -33.6$  dB and EEPN will be adjusted with the residual noise obtained.

Fig. 3 shows the OSNR measured after propagation for all configurations versus the varying power ( $P_{COI}$  for  $P_{1CH}$ ,  $P_{CUT}$ , and  $P_{FLAT}$ , and  $P_{WDM}$  for  $P_{ADJ}$ ). We observe that from -5 to 2.2 dBm, as expected,  $P_{1CH}$ ,  $P_{CUT}$ , and  $P_{FLAT}$  superpose, and  $P_{ADJ}$  stays constant as power of the adjacent channels is moving. For the nonlinear coefficients' estimation, we permanently remove var<sub>ASE</sub> (=1/SNR<sub>ASE</sub>) from var<sub>TOT</sub>.

Fig. 4 shows the COI's averaged  $SNR_{EXT}$  on all acquisitions versus the power. We observe that the curves for  $P_{1CH}$ ,



P<sub>CUT</sub>, and P<sub>FLAT</sub> superpose for low powers as ASE noise predominates. When reaching the regime where nonlinear effects have a higher impact (around 0dBm), the first configuration degraded is P<sub>CUT</sub> because of the adjacent highpower channels' strong XPM. Meanwhile, at low power, P<sub>ADJ</sub> is limited by the ASE noise of the COI, then degrades as the power of the adjacent channels increases and thus exhibits stronger XPM. P<sub>FLAT</sub>'s NLT is at 2.2 dBm. At this point, P<sub>CUT</sub>, P<sub>ADJ</sub>, and P<sub>FLAT</sub> have the same power profile; thus, the three curves superpose. After this point, P<sub>FLAT</sub> is slightly above P<sub>ADJ</sub> as the ASE noise is still predominating. However, they switch for higher power as they have equal XPM, but P<sub>FLAT</sub> has a higher SPM. After 2.2 dBm, P<sub>CUT</sub> and P<sub>1CH</sub> have similar behaviors. Around P<sub>FLAT</sub>'s NLT, P<sub>1CH</sub> is above as it does not have XPM, but they converge towards 10 dBm as SPM becomes predominant. Regarding the nonlinear coefficients; with the fit on P<sub>1CH</sub> and P<sub>CUT</sub>, we estimate the same  $\alpha_{SPM}^{P1CH}$  value, reported in Table 1. We also report  $\beta_{XPM}^{EXP}$  obtained with P<sub>ADJ</sub>, and the eGN model predictions. We note that the estimated coefficients are within +/-0.1 dB of the eGN model predictions. var<sub>res</sub> is then found at -33.4 dB, corresponding to 3.6% of the total noise contribution at P<sub>FLAT</sub>'s NLT. This residual noise could correspond to the estimated GAWBS and an estimated EEPN of -46.3 dB if an effective laser linewidth in the local oscillator of 7 kHz is considered, which is inline with the prediction in [6] using a similar offline transponder (var<sub>GAWBS</sub>+var<sub>EEPN</sub>(7kHz) = var<sub>res</sub>).

Table 1. Nonlinear coefficients obtained in experiments and with the eGN model and the deviation between them

	Exp	eGN	Deviation (dB)
α SPM	3.9*1e-04	4.0*1e-04	0.1 dB
$\beta_{XPM}$	6.5*1e-04	6.4*1e-04	-0.1 dB

Fig. 5 shows var<sub>TOT-ASE</sub> versus the power on the COI for  $P_{CUT}$ . We additionally plot the estimated XPM contribution with  $\beta_{XPM}^{EXP}$ , the estimated SPM contribution with  $\alpha_{SPM}^{EXP}$ , the estimated var<sub>res</sub>, and the prediction of SPM from the eGN model. Similarly, Fig. 6 shows var<sub>TOT-ASE</sub> for  $P_{ADJ}$ , the estimated XPM, SPM, var<sub>res</sub> contributions and the eGN prediction of XPM. On Fig. 4, we show for the four configurations the reconstructed model. The reconstructed model is the sum of the experimental ASE noise measurements, the estimated var<sub>res</sub>, and the estimated nonlinear effects with  $\beta_{XPM}$  and  $\alpha_{SPM}$  estimated with  $P_{ICH}$ ,  $P_{CUT}$ , and  $P_{ADJ}$ . We observe on Fig. 4 that the predicted SNR<sub>EXT</sub> for  $P_{FLAT}$  is very accurate while  $\alpha_{SPM}$  and  $\beta_{XPM}$  were obtained with only  $P_{ICH}$ ,  $P_{CUT}$ , and  $P_{ADJ}$ . Fig. 7 shows the deviation between the experiments SNR<sub>EXT</sub>, and the ones obtained with the reconstructed model versus the power for the four configurations. For all configurations, the mean error is below 0.1 dB, and the maximum error is within +/- 0.4 dB.



Fig. 5. Var<sub>TOT-ASE</sub> of P<sub>CUT</sub>, the estimated SPM, XPM and var<sub>res</sub> obtained with the fits and SPM predicted by the eGN model



Fig. 7. Deviation between the experimental  $SNR_{EXT}$  and the ones obtained with the estimated nonlinear coefficients and residual noise

### 5. Conclusions

We have experimentally measured the SPM and XPM fiber nonlinear coefficients in a highly dispersed QPSK transmission scenario. We tested the estimated values on different configurations to assess their reproductivity. We also compared them with the ones predicted by the eGN model. Both estimations are within +/-0.1 dB, showing a good agreement. On the other hand, we have isolated a residual noise that could correspond to GAWBS and EEPN.

### 6. References

[1] A. Carena, "EGN model of non-linear fiber propagation," Opt. Express 22, 16335-16362 (2014)

[2] J. Girard-Jollet, et. al., "Effective Impact of Modulation on Interchannel Nonlinear Effects in Realistic Submarine Links with Commercial Transceivers", ACP 2023

- [3] P. Ramantanis, et. al., "Uncertainty Aware Real-Time Performance Monitoring for Elastic Optical Networks," ECOC 2021
- [4] A. C. Meseguer, "Recent Progress in the Characterization of the GSNR and the OSNR of Future SDM-based Subsea Open Cables," OFC
- [5] J.-C. Antona et. al., "Analysis of 34 to 101GBaud Submarine Transmissions and Performance Prediction Models," OFC 2020
- [6] A. C. Meseguer, "Experimental characterization of equalization-enhanced phase noise in transoceanic transmission systems," ECOC 201